

# Estimating rock mass effective elastic properties from a Discrete Fracture Network (DFN) approach



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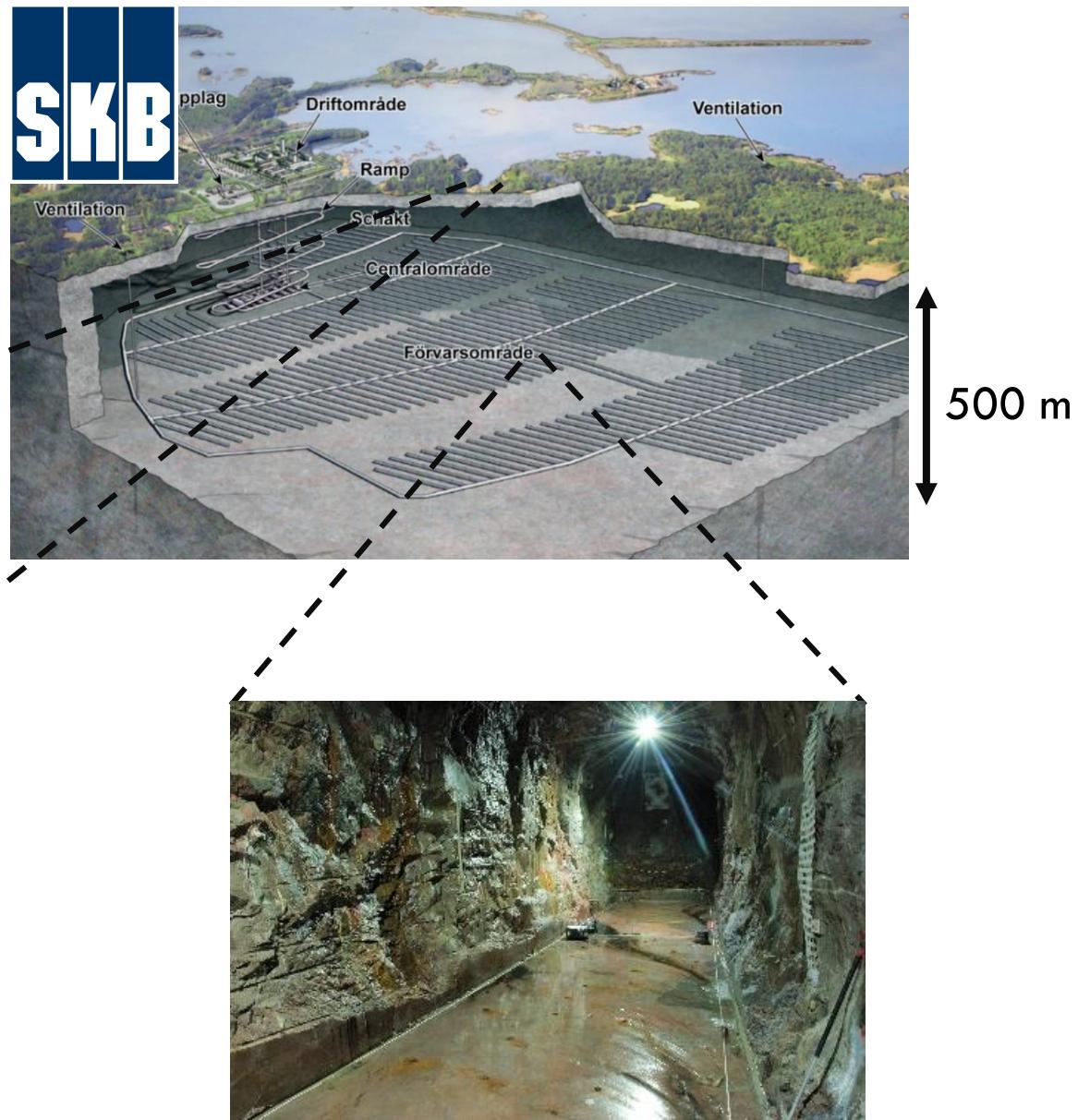
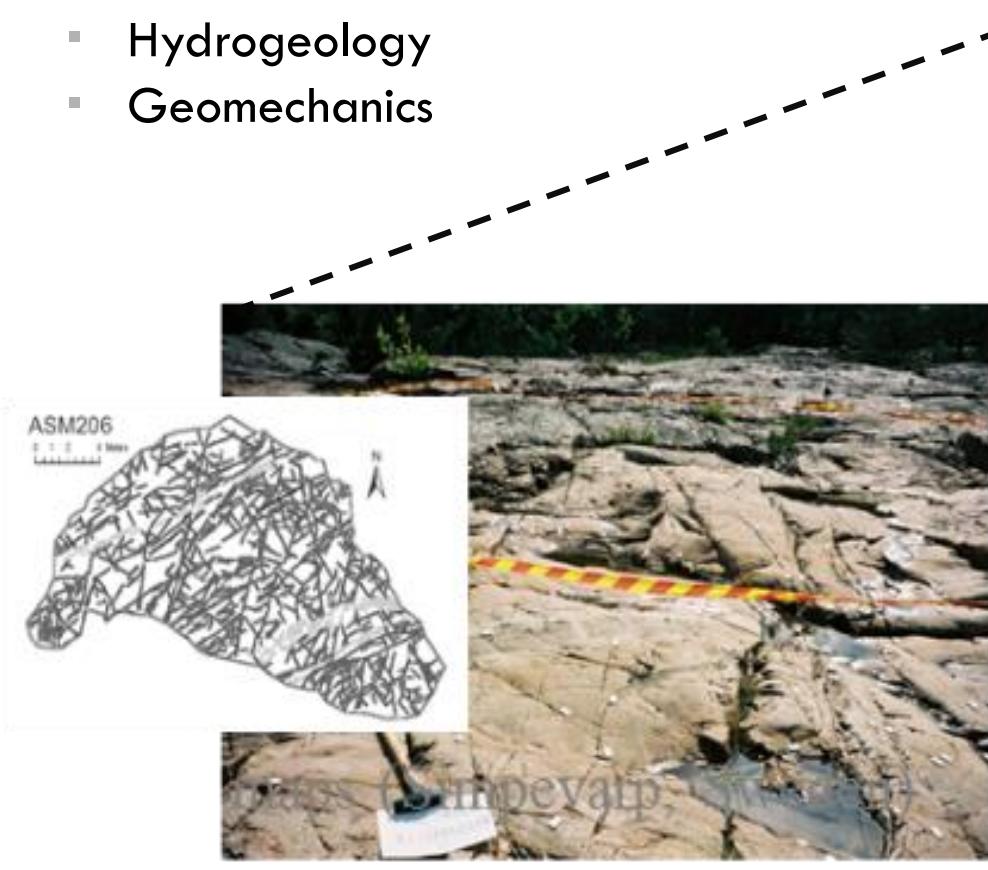
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# Introduction

## Context

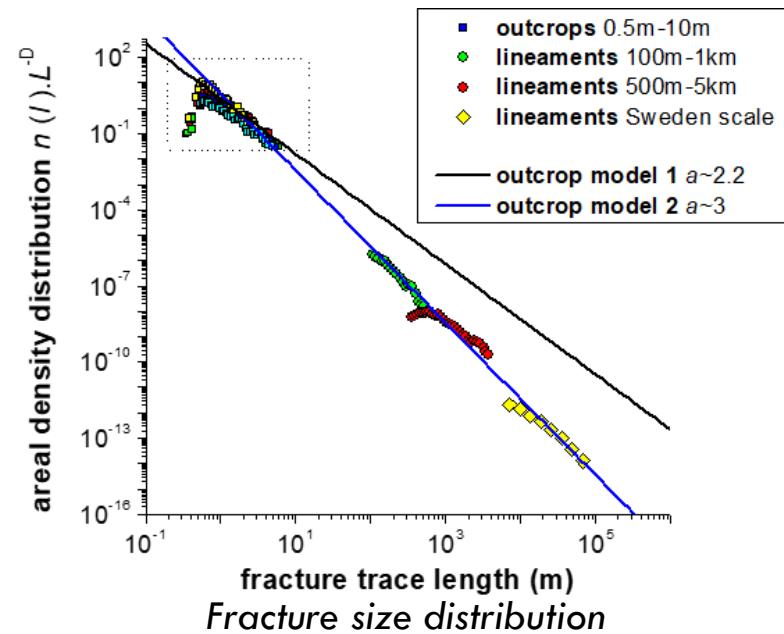
- Nuclear waste storage
- Crystalline rocks
- Fracture networks
- Hydrogeology
- Geomechanics



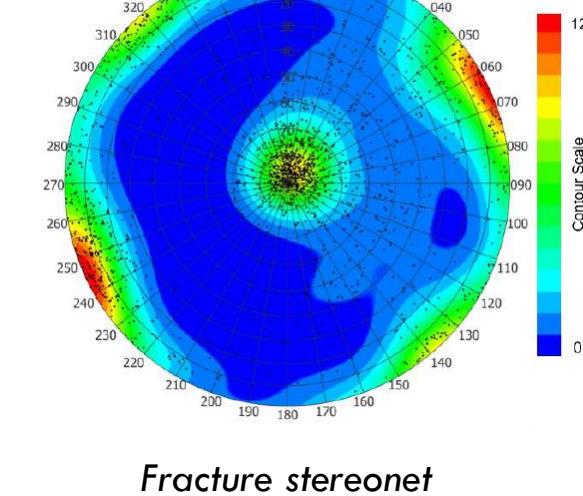
# Introduction

## Challenges

- Scale
  - Multiscale fracture networks (cm → km)
  - REV ?



- Anisotropy
  - Several fracture sets
  - Orientation distributions



Fracture stereonet

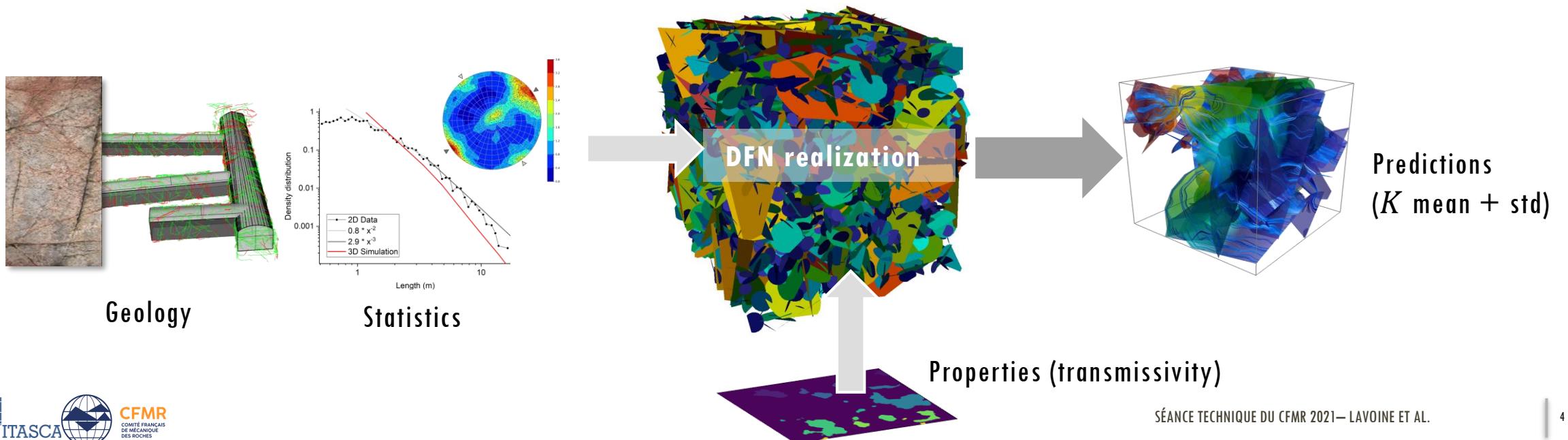
⇒ Fractures should be a central point of rock mass (RM) modelling  
⇒ DFN methodology

# Introduction

The Discrete Fracture Network (DFN) methodology [Selroos et al., 2021]

Fractured RM: population of deterministic and stochastic fracture-like objects embedded in an impervious elastic matrix

- Integrate geological, hydrogeological and mechanical data
- Valid regardless of fracture density
- Basis for simplification: effective properties, main hydro paths...
- And understanding: link with global indicators (percolation parameter...)



# Introduction

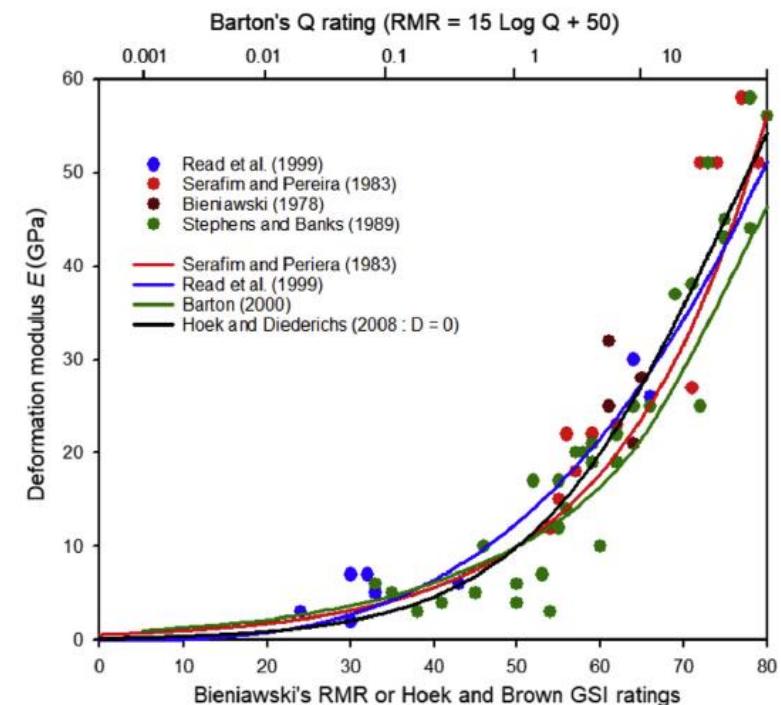
Applying the DFN methodology in geomechanics

To estimate fractured RM effective elastic properties

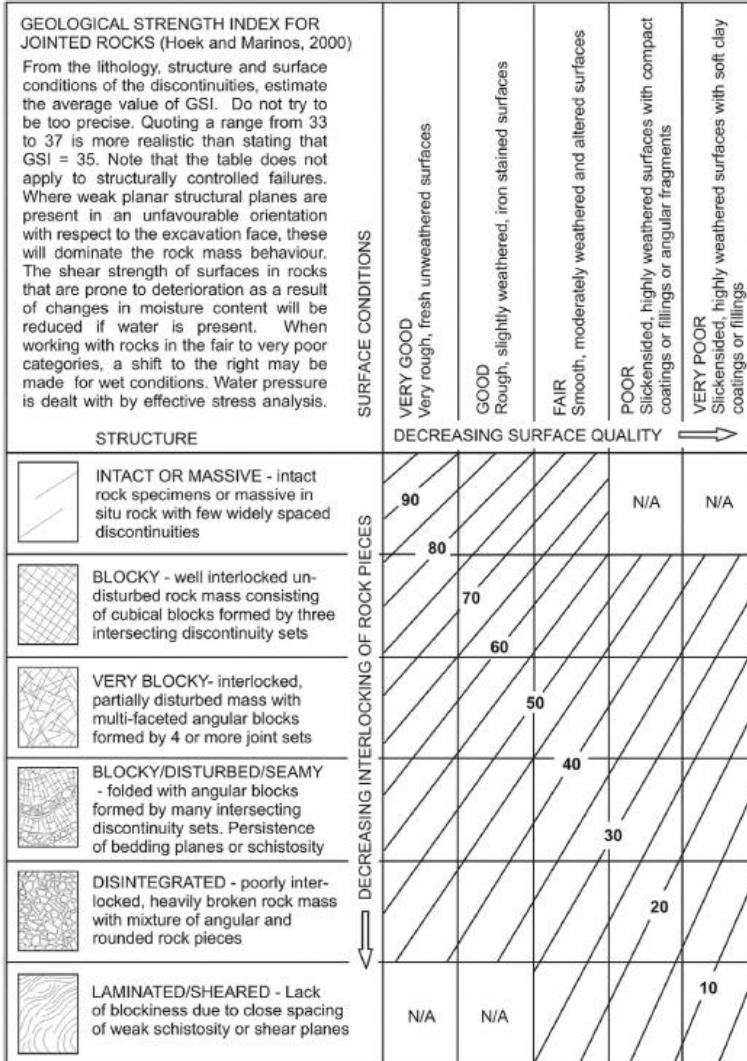
# Introduction

## Classically

- Rock Mass Classification (RMC) charts
- RQD, Q, RMR, GSI, D...
- Semi-empirical relationships



[Hoek and Brown (2018)]

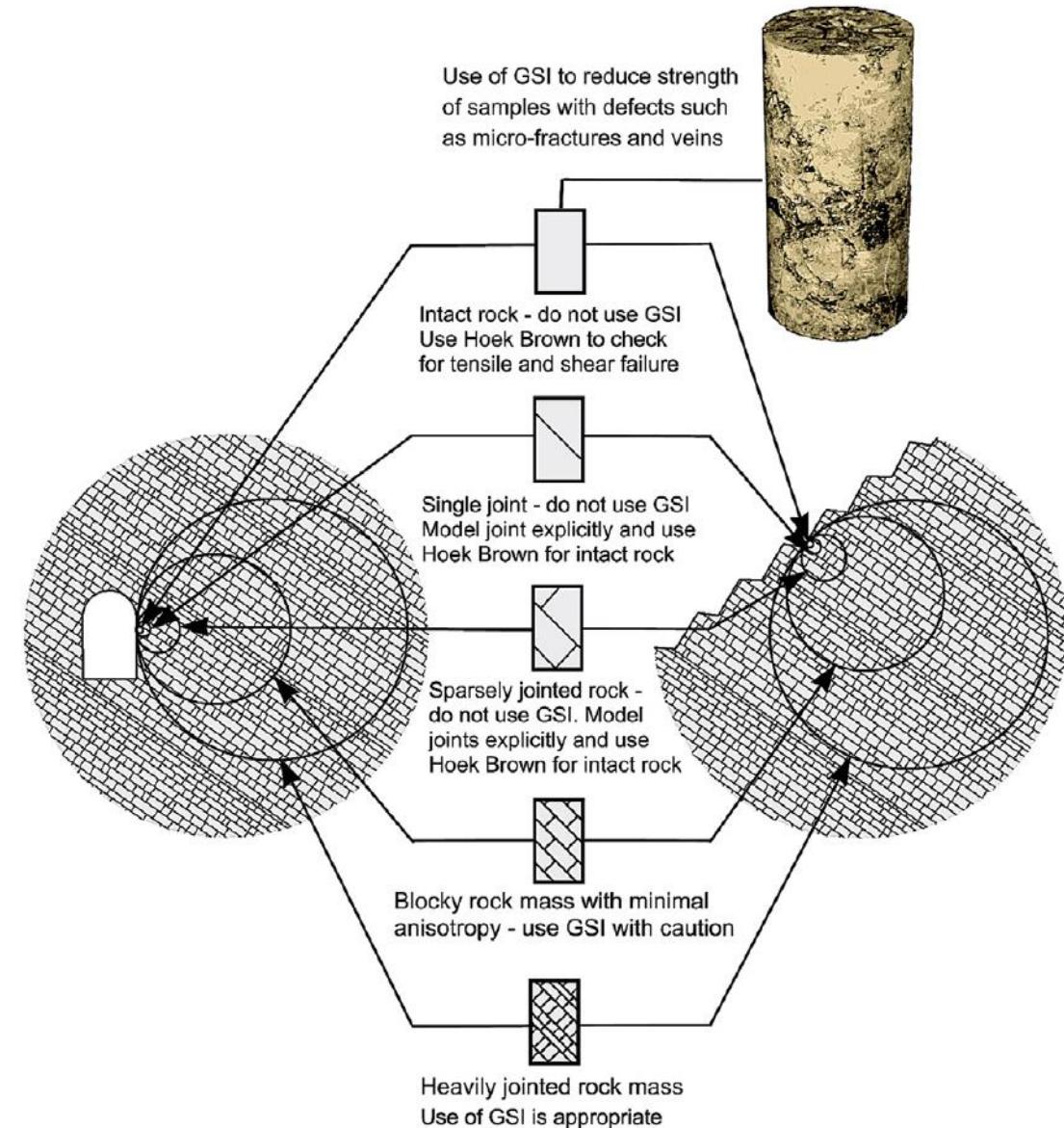


[Hoek and Marinos (2000)]

# Introduction

Adapted to heavily jointed rock masses

- Assembly of blocks
- Several sets of potentially infinite fractures
- Defined by fracture spacing only
- Applicable when model resolution  $\gg$  spacing



[Hoek and Brown (2018)]

# Introduction

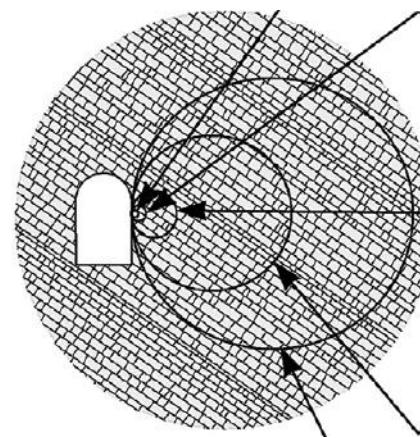
Adapted to heavily jointed rock masses

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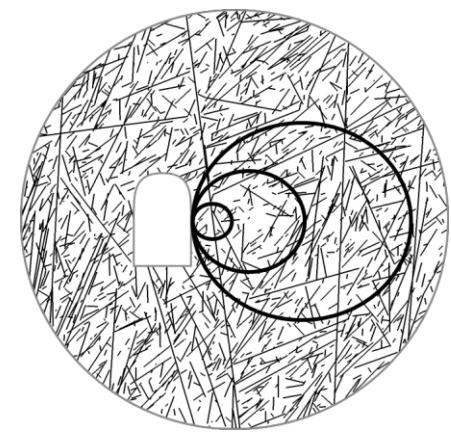
Lack of

- 3D representation
- Scale
- Anisotropy

⇒ DFN methodology



Block assembly



Population of individual fractures

# Introduction

## Objectives

- Overcome limitations of classical RMC approaches
- Using the DFN methodology to estimate RM effective elastic properties quantitatively

Effective compliance tensor

$$\bar{\bar{C}} = \bar{\bar{\epsilon}} : \bar{\bar{\sigma}}^{-1}$$

→ Total rock mass deformation

- Define which DFN metric is the controlling factor

# Fractures contribution to rock deformation

Total rock mass deformation : matrix deformation + contribution of all fractures

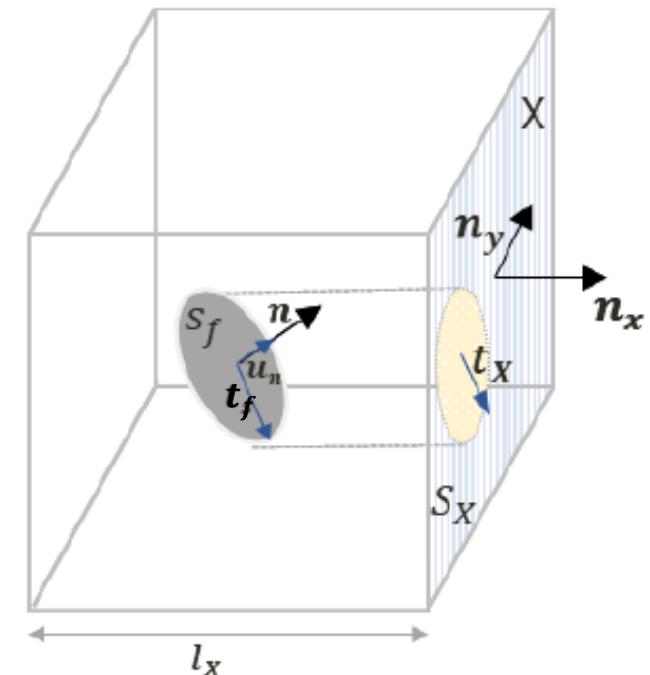
$$\epsilon_{ij} = C_{ijkl}^0 \sigma_{ij}^R + \sum_f (\epsilon_{ij})_f$$

Contribution of fracture  $f$  to the deformation component  $\epsilon_{xy}$

$$(\epsilon_{xy})_f = \frac{\mathbf{t}_X \cdot \mathbf{n}_y}{l_X} \rightarrow \text{Displacement / length}$$

$$\mathbf{t}_X = (\mathbf{n} \cdot \mathbf{n}_x) \frac{\int_{S_f} \mathbf{t}_f \cdot d\mathbf{S}}{S_X}$$

contribution of the fracture  $f$  to the displacement to the  $x$  boundary is obtained by projecting and integrating the displacement field on the  $x$  boundary



# Fractures contribution to rock deformation

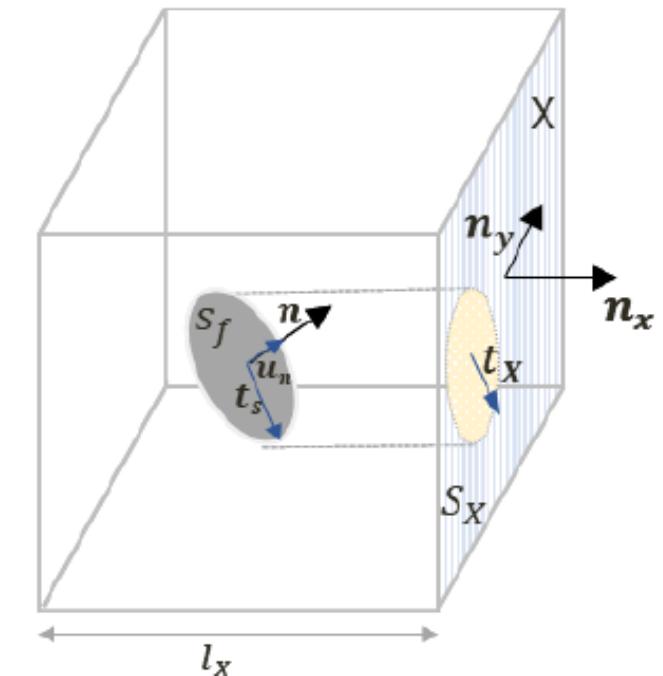
Total rock mass deformation : matrix deformation + contribution of all fractures

$$\epsilon_{ij} = C_{ijkl}^0 \sigma_{ij}^R + \sum_f (\epsilon_{ij})_f$$

Contribution of fracture  $f$  to the deformation component  $\epsilon_{xy}$

$$(\epsilon_{xy})_f = (\mathbf{n} \cdot \mathbf{n}_x) \frac{S_f}{V} (\bar{t}_f \cdot \mathbf{n}_y)$$

Fracture surface  
Rock volume  
mean shear fracture displacement



# Fractures contribution to rock deformation

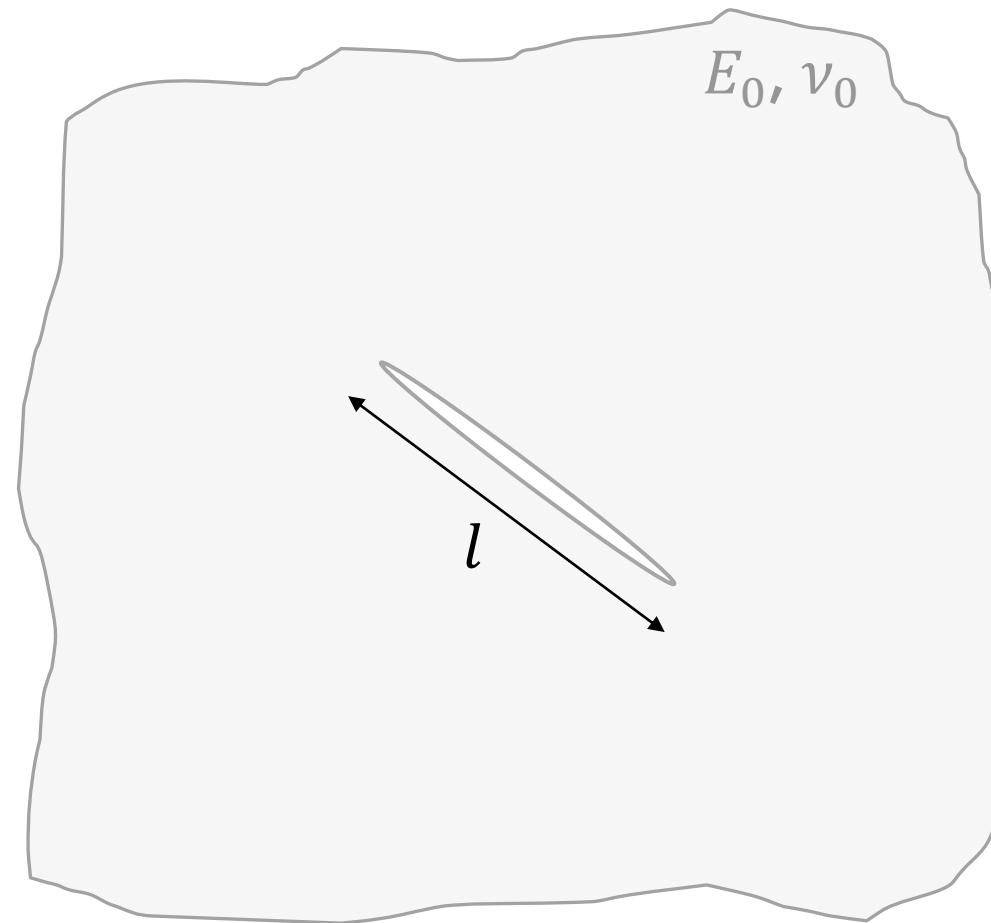
Mean shear displacement

Fracture of size  $l$

Elastic matrix

Intact Young modulus  $E_0$

Intact Poisson ratio  $\nu_0$



# Fractures contribution to rock deformation

Mean shear displacement

Matrix resistance to deformation

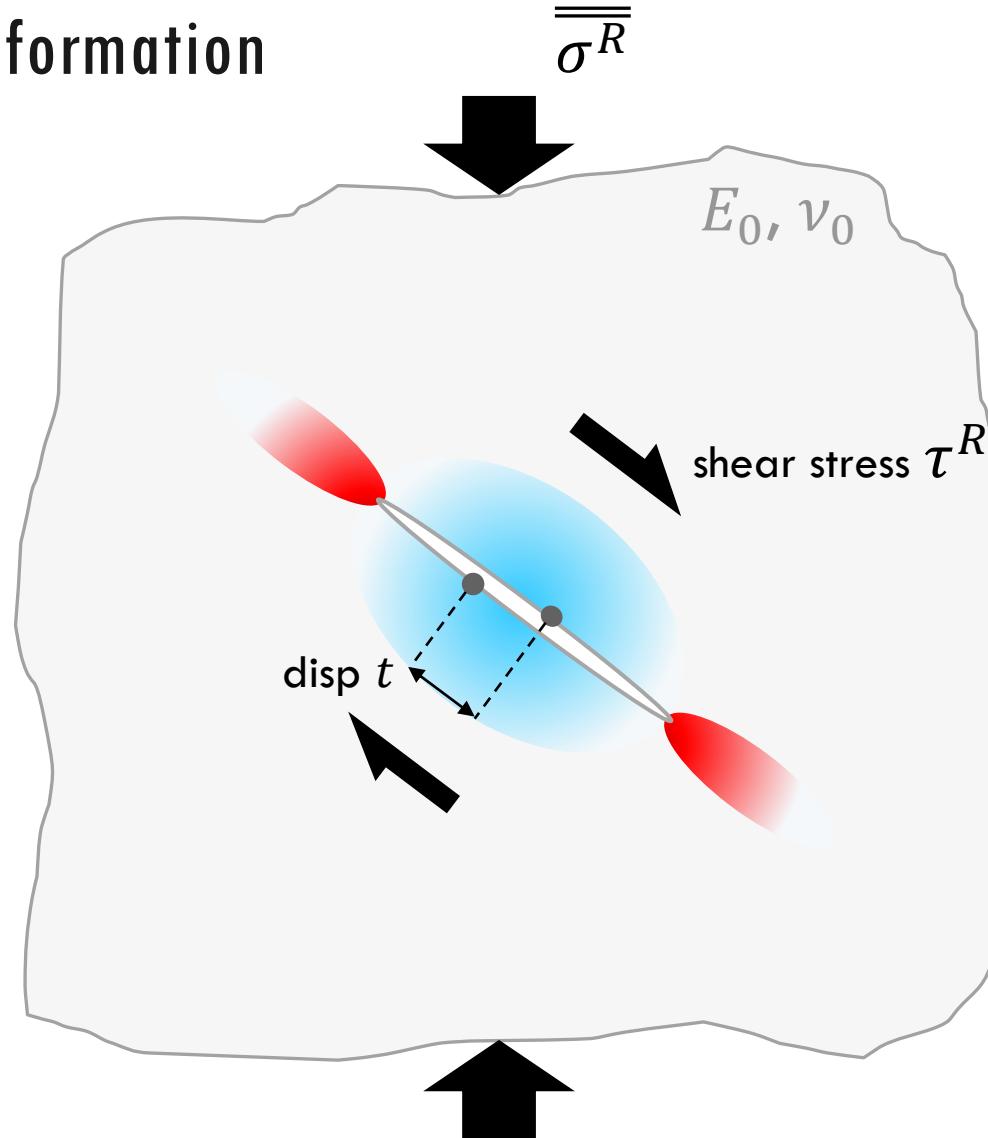
$$\tau_m = k_m \cdot t$$

Poisson ratio

Intact rock modulus

$$k_m = \frac{3\pi}{8} \cdot \frac{1 - \nu_0/2}{1 - \nu_0^2} \cdot \frac{E_0}{l} = \frac{E_m^*}{l}$$

Fracture size



$$\tau_R = \tau_m$$

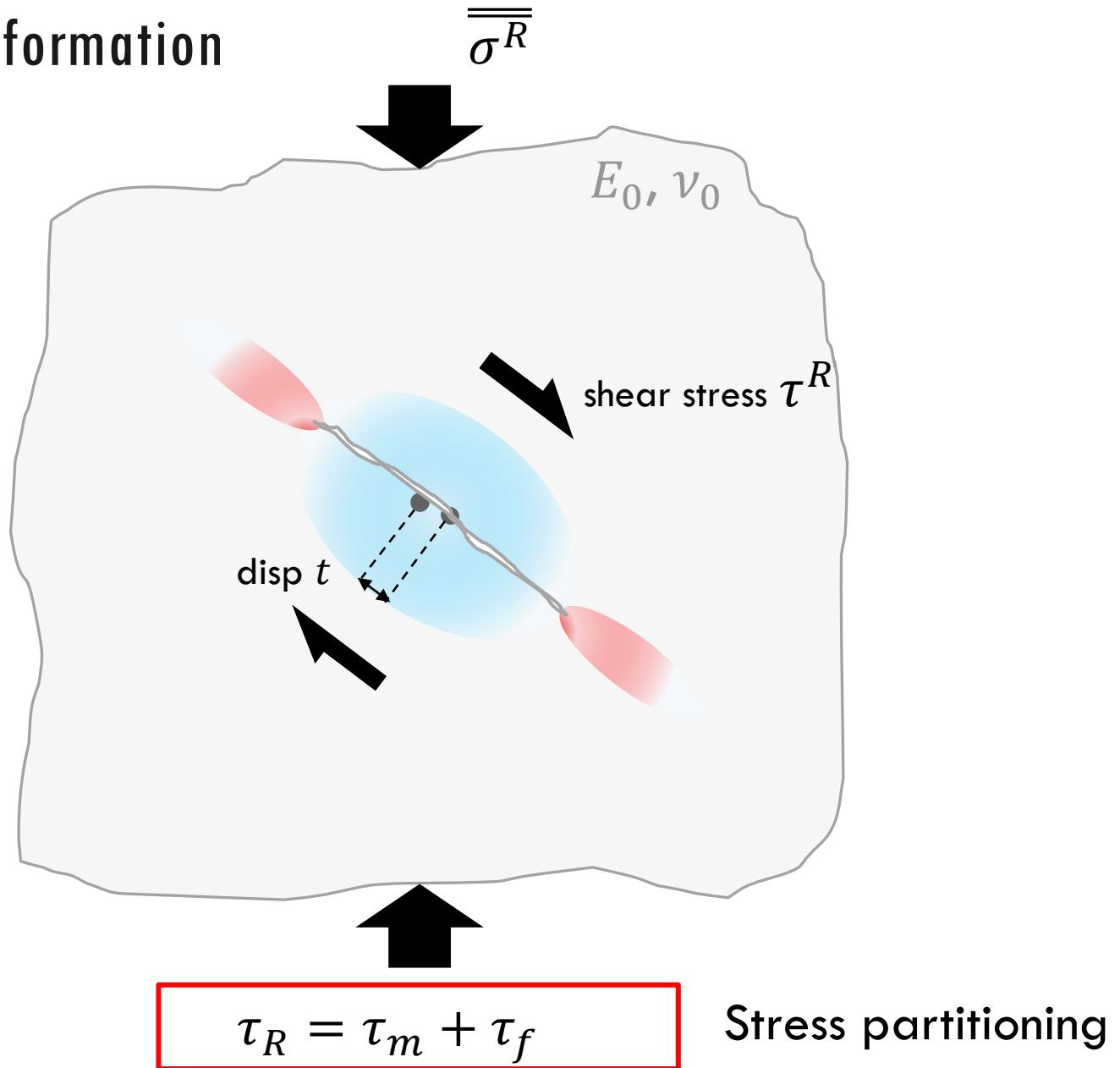
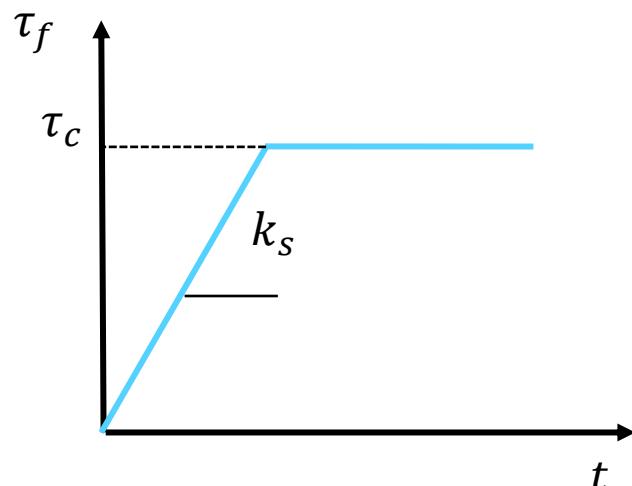
# Fractures contribution to rock deformation

Mean shear displacement

Fracture plane resistance

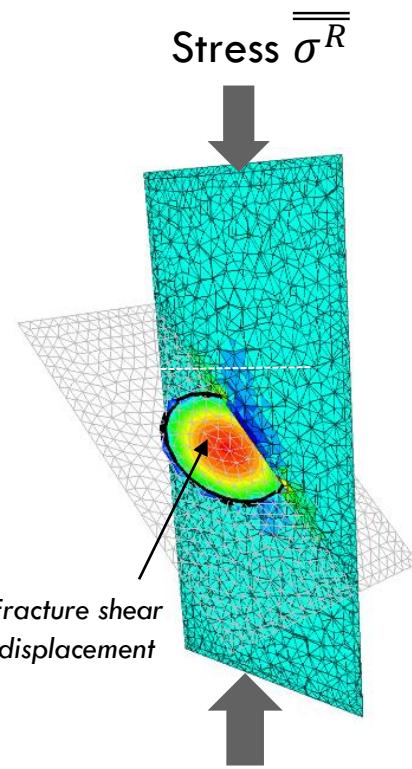
$$\tau_f = \min(k_s \cdot t, \tau_c)$$

Fracture shear stiffness      Coulomb stress limit  
(if critically stressed)



# Fractures contribution to rock deformation

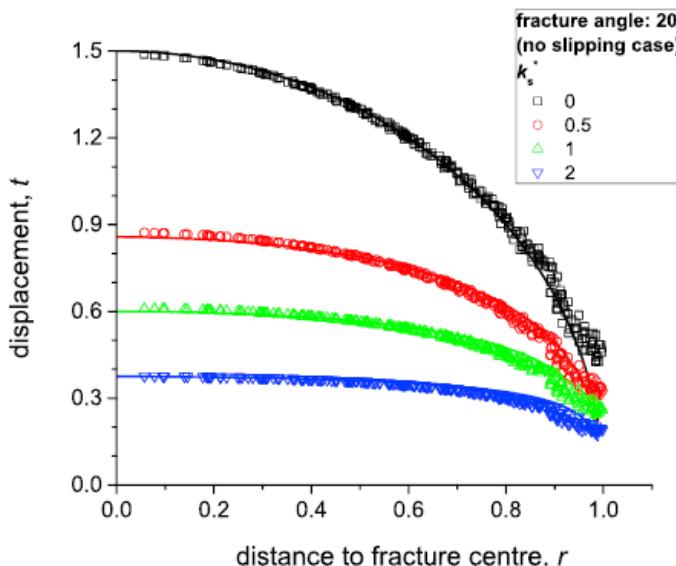
## Mean shear displacement



average

If not critically stressed

$$\frac{\tau^R}{t(r)} = \frac{\frac{2}{3}k_m}{\sqrt{1 - \left(\frac{2r}{l}\right)^2}} + k_s$$

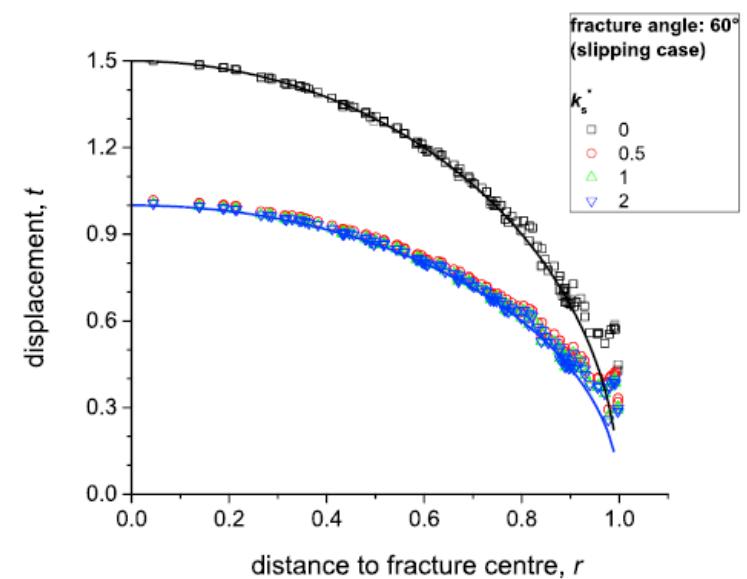


[Davy et al. (2018)]

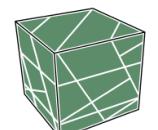
$$\bar{t} = \frac{\tau^R}{k_m + k_s}$$

If critically stressed

$$\frac{\tau^R - \tau_c}{t(r)} = \frac{\frac{2}{3}k_m}{\sqrt{1 - \left(\frac{2r}{l}\right)^2}}$$



$$\bar{t} = \frac{\tau^R - \tau_c}{k_m}$$



# Fractures contribution to rock deformation

## Scale dependency

With  $l_s = \frac{E_m^*}{k_s}$ , the fracture size so that  $k_m = k_s$

$$l \ll l_s \implies \bar{t} = \frac{\tau^R}{k_s + k_m} \approx \frac{\tau^R}{k_m} \propto l$$



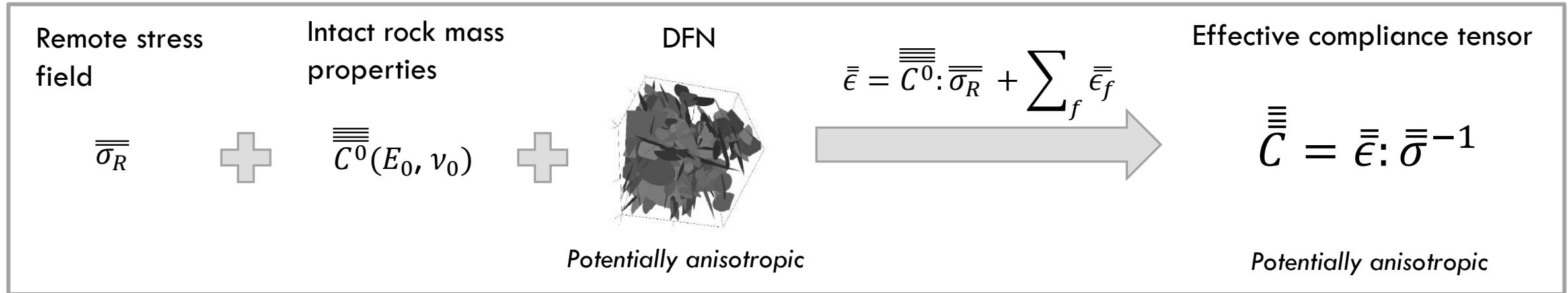
If  $k_s$  is negligible, fracture size defines the shear displacement

$$l \gg l_s \implies \bar{t} = \frac{\tau^R}{k_s + k_m} \approx \frac{\tau^R}{k_s}$$



If  $k_s$  is dominant, shear displacement is independent from fracture size

# Effective rock mass elastic properties



## Effective Theory:

Fracture  $f$  « sees » a matrix damaged by  
[1,  $(f - 1)$ ] fractures

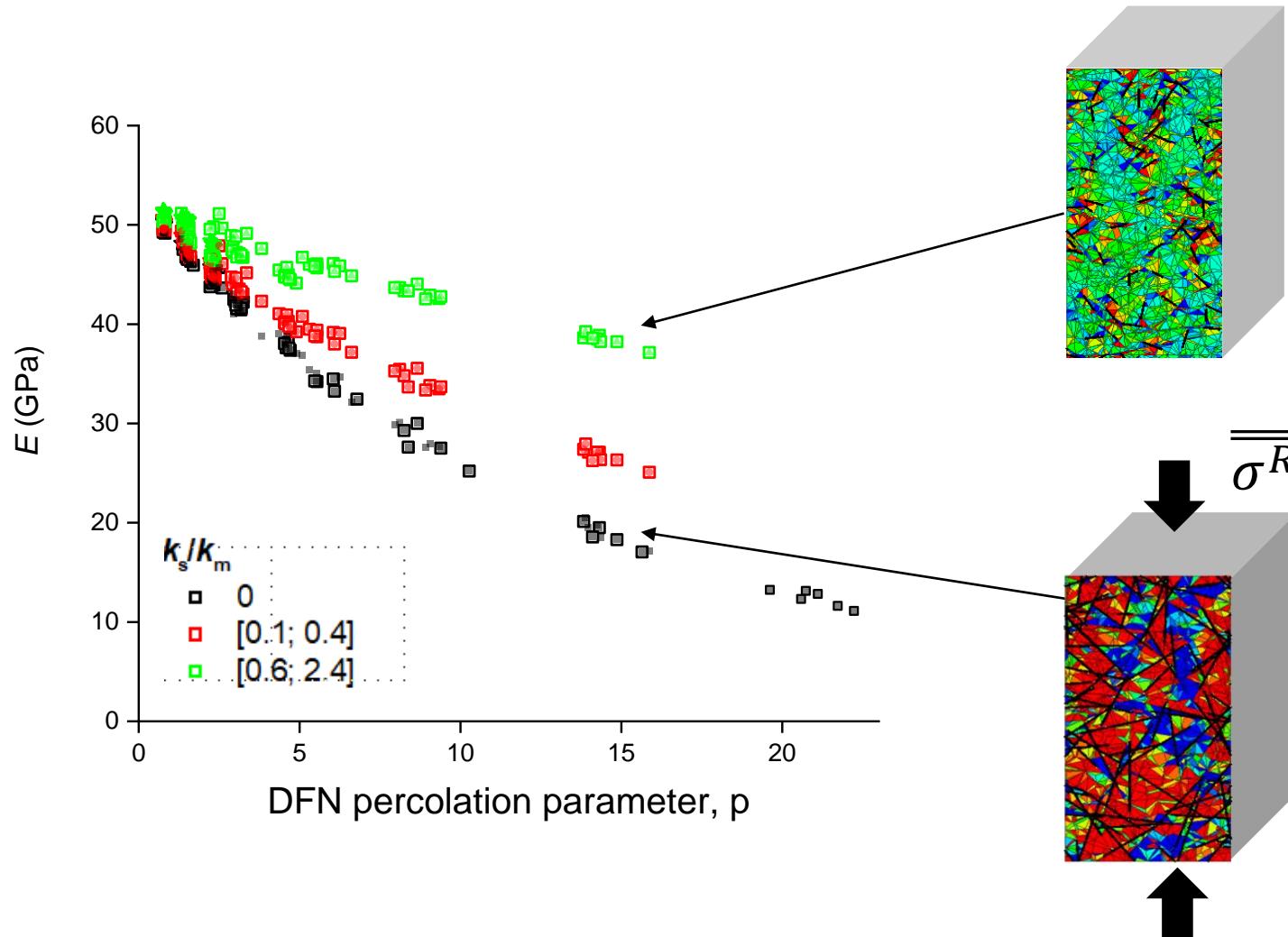
Loop for all fractures

$$E_{f-1} = \frac{1}{3} \left( \frac{1}{E_{xx,f-1}} + \frac{1}{E_{yy,f-1}} + \frac{1}{E_{zz,f-1}} \right)$$

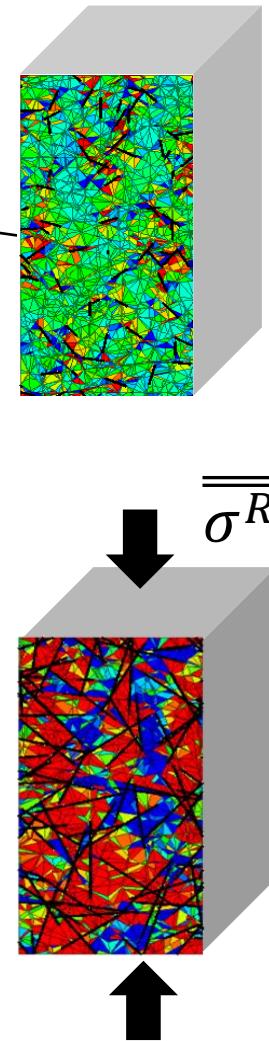
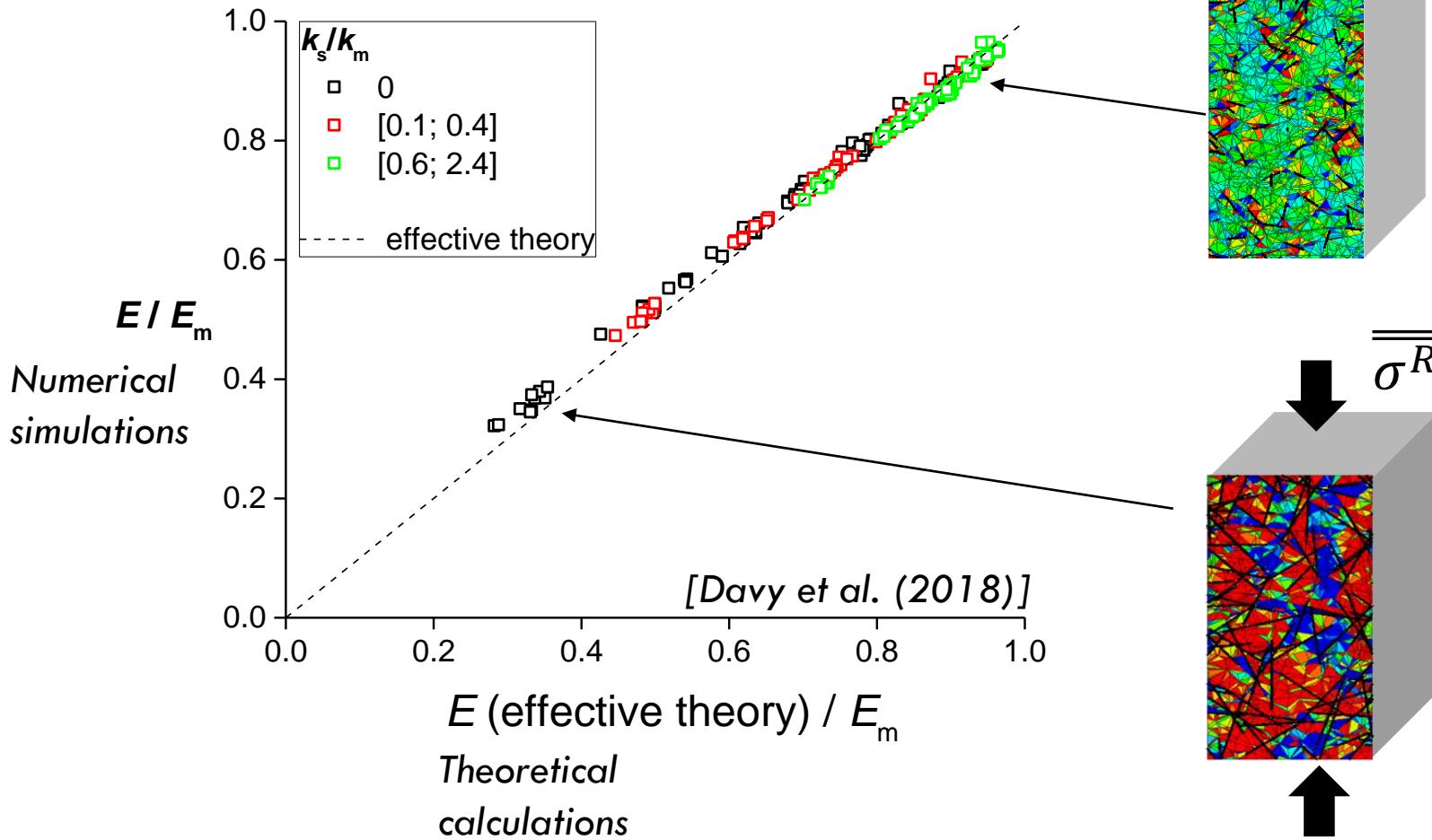
$$t_f = \frac{\tau}{k_s + \frac{E_{f-1}^*}{l_f}}$$

$$E_{xx,f}, E_{yy,f}, E_{zz,f}$$

# Effective rock mass elastic properties



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# Effective rock mass elastic properties

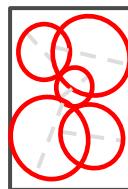
Analytical solutions for simple cases

- If  $k_s \ll k_m$  ( $l \ll l_s$ )

$$E_{eff} = E_m \exp(-c(\theta)p)$$

$$p = \frac{1}{V} \sum_f l_f^3$$

So-called percolation parameter

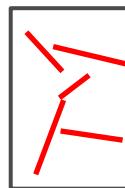


Potential size effect since  
 $p$  is scale dependent

- If  $k_s \gg k_m$  ( $l \gg l_s$ )

$$E_{eff} \sim \frac{k_s}{P_{32} + k_s/E_m}$$

$$P_{32} = \frac{1}{V} \sum_f l_f^2$$

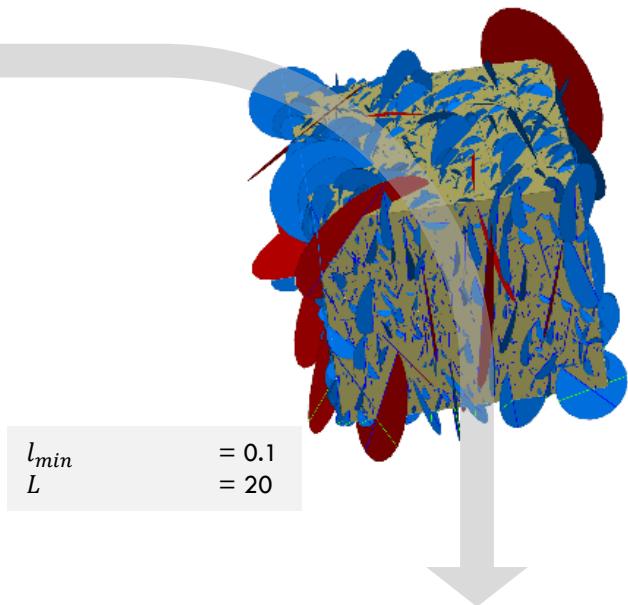
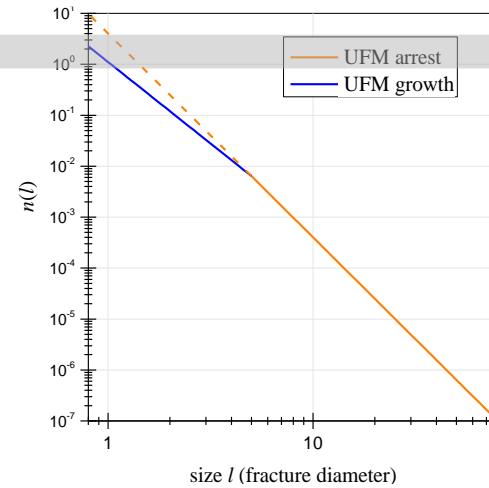
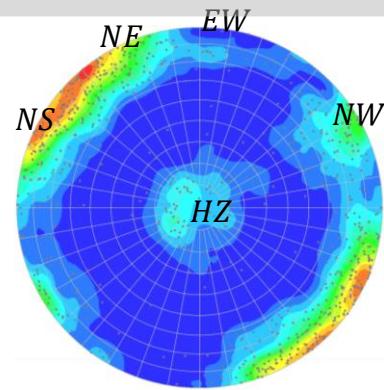


No size effect since  
 $P_{32}$  is scale independent

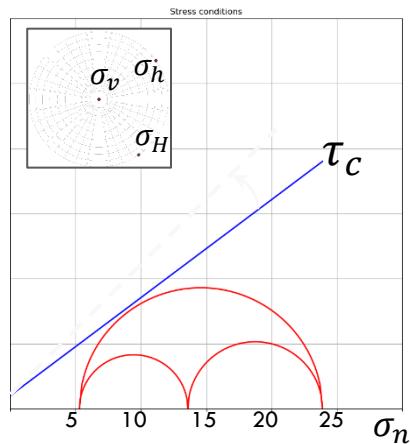
Total fracture surface per unit volume

# Application to Forsmark FFM01 deformation zone

DFN (FFM01 unit)



## Mechanical properties



No critically stressed fractures

### Intact Rock

$$E_m = 76 \text{ GPa}$$

$$\nu_m = 0.23$$

### Fractures

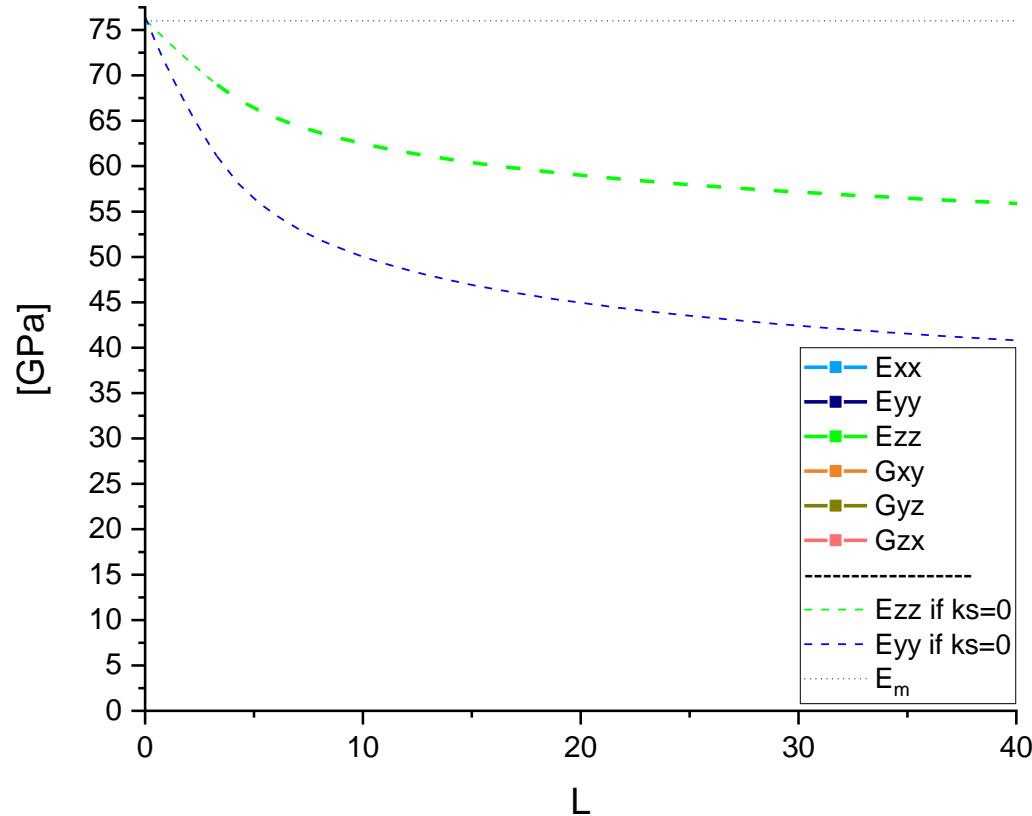
$$k_s(\sigma_n) = 46.55 \times \sigma_n^{0.4039} \times 10^6$$

$$k_n > 100k_s$$

$$\begin{bmatrix} \epsilon_x \\ \epsilon_y \\ \epsilon_z \\ \epsilon_{yz} \\ \epsilon_{xz} \\ \epsilon_{xy} \end{bmatrix} = \begin{bmatrix} \frac{1}{E_{xx}} & -\frac{\nu_{yx}}{E_y} & -\frac{\nu_{zx}}{E_z} & 0 & 0 & 0 \\ -\frac{\nu_{xy}}{E_x} & \frac{1}{E_y} & -\frac{\nu_{zy}}{E_z} & 0 & 0 & 0 \\ -\frac{\nu_{xz}}{E_x} & -\frac{\nu_{yz}}{E_y} & \frac{1}{E_z} & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{1}{2G_{yz}} & 0 & 0 \\ 0 & 0 & 0 & 0 & \frac{1}{2G_{xz}} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{1}{2G_{xy}} \end{bmatrix} \times \begin{bmatrix} \sigma_x \\ \sigma_y \\ \sigma_z \\ \tau_{yz} \\ \tau_{xz} \\ \tau_{xy} \end{bmatrix}$$

Compliance tensor  $\bar{\mathcal{C}}$

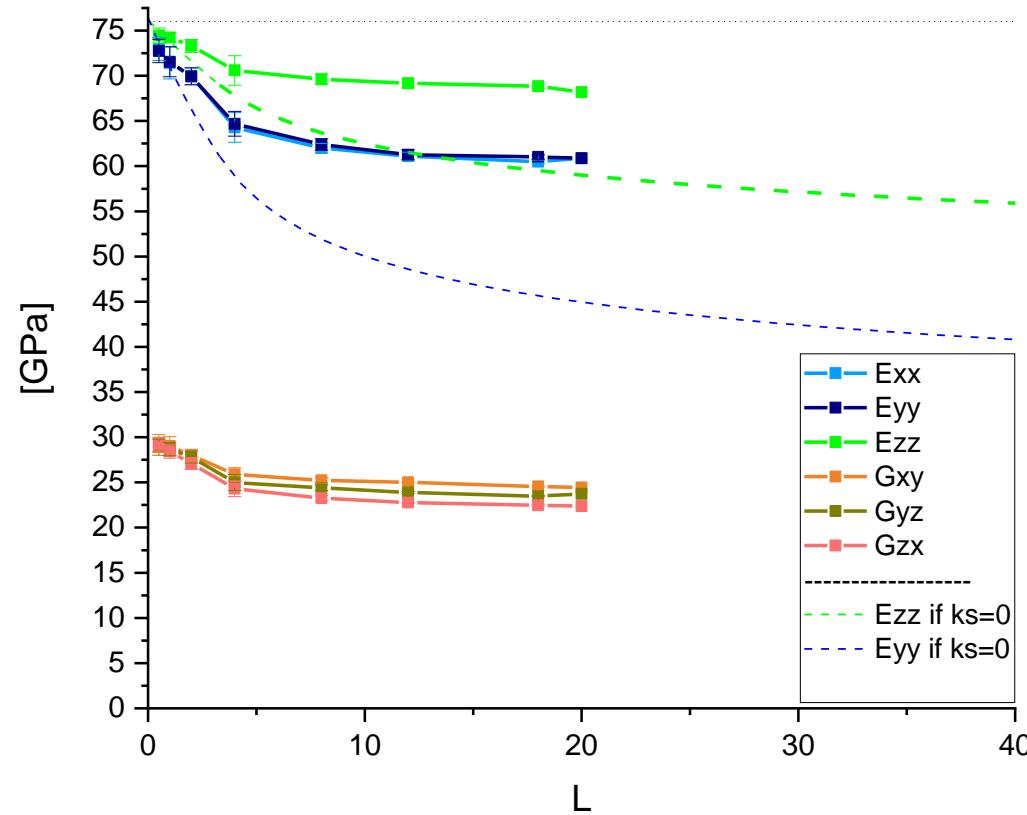
# Application to Forsmark FFM01 deformation zone



Given the DFN conditions:

- If  $k_s = 0 \rightarrow$  maximise the scaling effect

# Application to Forsmark FFM01 deformation zone



Given the DFN conditions:

- If  $k_s = 0 \rightarrow$  maximise the scaling effect

With current mechanical properties

- $1.5 \text{ m} \leq l_s \leq 3.5 \text{ m}$
- Decrease of  $E_{ii}$  with  $L$  up to  $\sim 10\text{m}$ .
- $E_{xx}$  decrease from 76 Gpa to about 62 GPa, i.e. about 25%.

# Conclusion

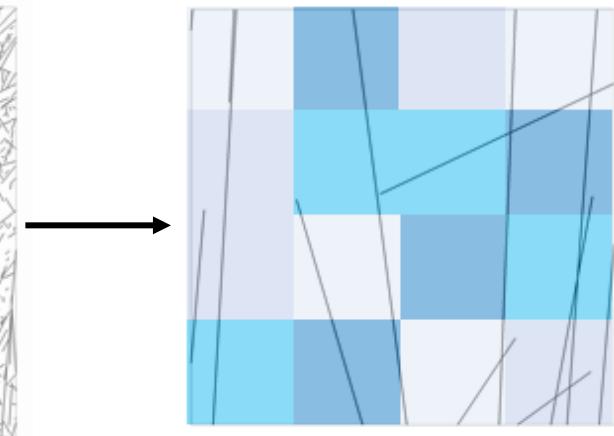
- DFN methodology: integrate multiscale anisotropic fracture distributions
- Effective elastic properties of fractured RM can be assessed quantitatively by a method combining individual fractures contributions
- The developed method can be applied to large DFN (million of fractures)
- Fracture frictional properties introduce scales effects
- Depending on fracture frictional properties (ratio  $l/l_s$ ) the effective properties are driven either by  $p$  or  $P_{32}$

# Perspective

- Comparison with predictions based on RMC charts
- Characterization of stress fluctuations, and associated scale dependence
- Semi-effective medium representation
- Extend the methodology to strength properties



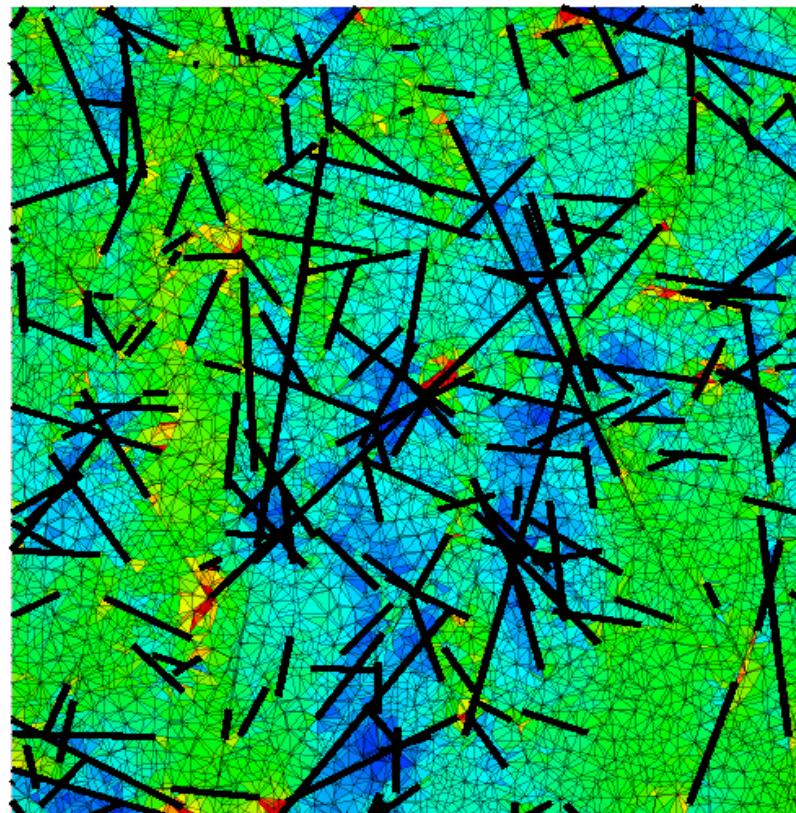
*Full DFN*



*Semi-effective medium*

# Conclusion

# Thanks for your attention



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